

Total No. of Questions—8]

[Total No. of Printed Pages—4

Seat No.	
-------------	--

[5668]-201

S.E. (Information Technology) (Third Semester) EXAMINATION, 2019
DISCRETE STRUCTURES
(2015 PATTERN)

Time : Two Hours

Maximum Marks : 50

- N.B. :— (i) Solve Q. Nos. 1 or 2, 3 or 4, 5 or 6, 7 or 8.
(ii) Neat diagrams must be drawn wherever necessary.
(iii) Figures to the right indicate full marks.
(iv) Assume suitable data, if necessary.

1. (a) A bag contains 3 red, 6 white and 7 blue balls. What is the probability that two balls drawn are white and blue ? [6]
(b) Three cards are drawn from a well-shuffled pack of 52 cards. Find the probability that they are a king, a queen and a jack. [6]

Or

2. (a) How many 3-digit numbers can be formed from the digits 2, 3, 5, 6, 7 and 9, which are divisible by 5 and none of the digits is repeated ? [6]
(b) What is Multiset ? Let A and B be the multisets {a, a, b, b, c, f} and {a, a, b, b, b, d, d}, respectively. [6]

Find :

- (a) $A \cup B$
(b) $A \cap B$
(c) $A - B$
(d) $B - A$.
3. (a) Prove by Mathematical Induction that for $n \geq 1$: [6]
 $1.1! + 2.2! + 3.3! + \dots + n.n! = (n+1)!$

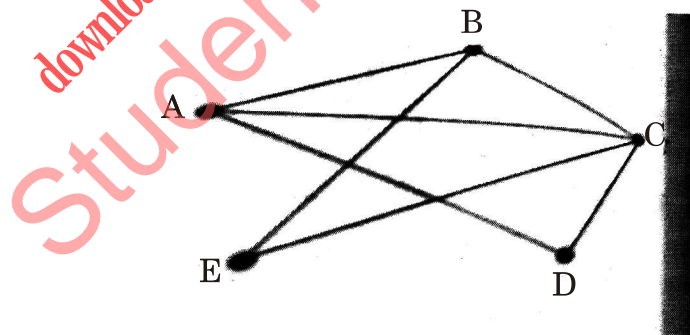
P.T.O.

- (b) Define with example : [6]
- (i) Equivalence relation
 - (ii) POSET
 - (iii) Lattice.

Or

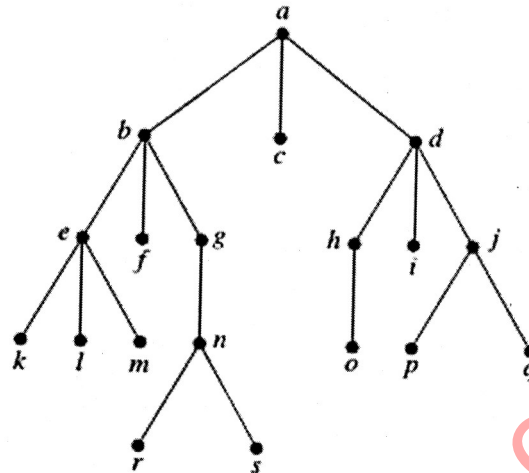
4. (a) Solve the following recurrence relation : [6]
- $$x(n) - 6x(n-1) + 9x(n-2) = 0$$
- $$x(0) = 0$$
- $$x(1) = 3.$$

- (b) Consider the graph given in the figure, find the set $V(G)$ of the vertices present in G and that set $E(G)$ of edges of G also find the degree of each vertex and show that sum of the degree of the vertices is twice the number of edges in graph G . [6]



5. (a) Build a binary search tree for the words banana, peach, apple, pear, coconut, mango and papaya using alphabetical order. Write sequence of visiting words in preorder and post-order traversal. [7]

- (b) Determine the order in which a preorder, postorder and inorder traversal visits the vertices of the given ordered rooted tree. [6]



Or

6. (a) What is expression tree ?

Represent the expressions

(i) $(x + xy) + (x/y)$

(ii) $x + ((xy + x)/y)$

[7]

using binary trees. Write each of these expressions in :

(a) prefix notation.

(b) postfix notation.

- (b) For the following set of characters, construct Huffman code.

Find average bit length of the code :

[6]

Character	A	B	C	D	E
Frequency	0.1	0.15	0.25	0.2	0.3

7. (a) Let $G = \{\text{even, odd}\}$ and binary operation \oplus be define as : [7]

\oplus	even	odd
even	even	odd
odd	odd	even

Show that (G, \oplus) is a group.

- (b) Define the following : [6]

- (a) Group
- (b) Monoid
- (c) Abelian group.

Or

8. (a) Show that $(G, +_g)$ is an abelian group where $G = \{0, 1, 2, 3, 4, 5, 6, 7\}$. [7]
- (b) Prove that $G = \{0, 1, 2, 3, 4, 5\} = Z_6$ is an abelian group of order 6 with respect to addition modulo 6. [6]